Studying Mathematical Relationships Using TI Calculator

Carneathea Melson
The College at Brockport

Follow this and additional works at: http://digitalcommons.brockport.edu/cmst_lessonplans

Part of the Physical Sciences and Mathematics Commons, and the Science and Mathematics Education Commons

Repository Citation
http://digitalcommons.brockport.edu/cmst_lessonplans/226

This Lesson Plan is brought to you for free and open access by the CMST Institute at Digital Commons @Brockport. It has been accepted for inclusion in Lesson Plans by an authorized administrator of Digital Commons @Brockport. For more information, please contact kmyers@brockport.edu.
CMST SCOLLARCITY Lesson Plan Template-Lesson Plan using **TI Technologies**
(Due Tuesday, July 27th)

Submit as hard copy AND electronically through ANGEL

<table>
<thead>
<tr>
<th>Name: Carneathea Melson</th>
</tr>
</thead>
<tbody>
<tr>
<td>Grade level(s)/Subject taught: 10 – 12/ Algebra II Honors</td>
</tr>
</tbody>
</table>

**Objectives:** (Remember…How will the modeling tool help the student better learn the objective?) The student will learn how to choose a mathematical model (linear, quadratic, exponential, and trigonometric) to model real world data. Students will be able to make predictions from the data.

Items to include in your TI Technologies lesson plan: (use your area/discipline/concepts).

**For the math teacher:**

1. Write the Mathematical Concept or “key idea” that TI Technologies will be used to teach: (e.g. Students use mathematical modeling/ multiple representation to provide a means of presenting, interpreting, communicating, and connecting mathematical information and relationships)

Students use mathematical modeling/ multiple representation to provide a means of presenting, interpreting, communicating, and connecting mathematical information and relationships. They will be able to use the graphic calculator to model the data and choose proper mathematic model to simulate the data.

Real world data most often cannot be modeled precisely with a single equation. Mathematicians, scientists and engineers still need to be able to make predictions from the data. They need to find functions to fit data. It will be the students’ job to write an equation of an actual real-world situation.

Using TI 83/84 graphing calculator, I plan to have students plot the data of the daily high temperature in New Orleans, Louisiana for several days of a given year. The students will then write a cosine model for the data using the formula \( y = a \cos b(x - h) + k \). Next the students’ job will be to determine the amplitude, period, horizontal shift and vertical shift (a, b, h and k respectively) from the given data. Then the student will input the equation into the calculator and graph the equation to determine if it fits the data. Once a proper equation is modeled, then the student will use it to estimate the temperature in New Orleans on Sept. 1 (day 244) or any day of that year.

To accomplish this task, prior lessons on finding the amplitude, period and translating trigonometric function will have been taught. I would open the lesson with a 10 minute bell work assignment. Students will demonstrate above knowledge by solving various problems.
on the translation of the graph “$y = \sin x$” in the interval $0 \leq x \leq 2\pi$ on the graphing

calculator. The following problems will be given: $y = 2 \sin x + 3$, $y \sin(x - \frac{\pi}{2})$ and

$f(x) = \sin(x + \pi) - 2$. Students will have to graph the equations and identify the amplitude,
cycle, horizontal and vertical shifts of each. Three students will be chosen to demonstrate
graphs on the overhead and answer the above questions. They will receive bonus points
towards their homework grades.

**LESSON**

The data from the table is

<table>
<thead>
<tr>
<th>Day of Year</th>
<th>Temperature (°F)</th>
</tr>
</thead>
<tbody>
<tr>
<td>16</td>
<td>62</td>
</tr>
<tr>
<td>47</td>
<td>65</td>
</tr>
<tr>
<td>75</td>
<td>71</td>
</tr>
<tr>
<td>106</td>
<td>79</td>
</tr>
<tr>
<td>136</td>
<td>85</td>
</tr>
<tr>
<td>167</td>
<td>90</td>
</tr>
<tr>
<td>197</td>
<td>91</td>
</tr>
<tr>
<td>228</td>
<td>90</td>
</tr>
<tr>
<td>259</td>
<td>87</td>
</tr>
<tr>
<td>289</td>
<td>79</td>
</tr>
<tr>
<td>320</td>
<td>70</td>
</tr>
<tr>
<td>350</td>
<td>64</td>
</tr>
</tbody>
</table>

put into the graphing

calculator using the STAT, EDIT
button. This will take about 5 minutes.

Next the student will graph data using

STAT PLOT.

For the remainder of the period (25 minutes) do the following calculations.

*To find the amplitude (a) use the formula $a = \frac{1}{2}(\text{max} - \text{min})$

$$a = \frac{1}{2}(91 - 62)$$

$$a = 14.5$$

*To find the cycle (b) use the formula $\text{period} = \frac{2\pi}{b}$. One complete cycle takes 365 days.

$$365 = \frac{2\pi}{b}$$

Now solve for b.

$$b = \frac{2\pi}{365}$$

Now substitute $a$ and $b$ into the equation $y = a \sin b x$ to obtain $y = 14.5 \cos \frac{2\pi}{365} x$. 
*To find the translation values \( h \) and \( k \), compare \( y = 14.5 \cos \frac{2\pi}{365} x \) with the plot of the data.

**Phase shift (horizontal shift):** \( h = 197 - 0 = 197 \)

**vertical shift:** \( k = 91 - 14.5 = 76.5 \)

*Using the formula \( y = a \cos b(x - h) + k \) write the final equation.

The model for the data is \( y = 14.5 \cos \frac{2\pi}{365}(x - 197) + 76.5 \). Input equation to see if data fits.

**NOTE:** Make sure you are in radian mode.

*Now students can estimate the temperature for day 244. Go to trace, make sure the equation shows at the top of the graph, then put in 244 for \( x \) to find the value for \( y \). The value for the high temperature for Sept. 1st is 86.5 degrees.
Assessment

To assess the learning I will give students a homework assignment which uses a sine function to model the normal daily high temperature in New Orleans. Use the equation \( y = a \sin b(x - h) + k \). Then use the sine model to estimate the high temperature on Sept 1 (day 244).

<table>
<thead>
<tr>
<th>Day of the year</th>
<th>16</th>
<th>47</th>
<th>75</th>
<th>106</th>
<th>136</th>
<th>176</th>
<th>197</th>
<th>228</th>
<th>259</th>
<th>289</th>
<th>320</th>
<th>350</th>
</tr>
</thead>
<tbody>
<tr>
<td>Temperature</td>
<td>71</td>
<td>69</td>
<td>70</td>
<td>73</td>
<td>77</td>
<td>82</td>
<td>85</td>
<td>86</td>
<td>84</td>
<td>82</td>
<td>78</td>
<td>74</td>
</tr>
</tbody>
</table>

Students will be graded based upon their calculations and final equations. They will have to show the actual simulation on the graphing calculator to receive a passing grade. If they have all the components that we had above and the simulation they will receive 10 points. If they show only calculations without the simulation, they will only receive 5 points.